

Corrigé de l'exercice 1

Calculer les expressions suivantes et donner le résultat sous la forme d'une fraction irréductible.

$$A = \frac{\frac{2}{5} + 6}{\frac{-7}{9} - 7}$$

$$A = \frac{\frac{2}{5} + \frac{6 \times 5}{1 \times 5}}{\frac{-7}{9} - \frac{7 \times 9}{1 \times 9}}$$

$$A = \frac{\frac{2}{5} + \frac{30}{5}}{\frac{-7}{9} - \frac{63}{9}}$$

$$A = \frac{32}{5} \div \frac{-70}{9}$$

$$A = \frac{32}{5} \times \frac{-9}{70}$$

$$A = \frac{16 \times 2}{-5 \times -1} \times \frac{9 \times -1}{35 \times 2}$$

$$A = \boxed{\frac{-144}{175}}$$

$$B = \frac{9}{2} \div \left(\frac{1}{11} + \frac{-1}{13} \right)$$

$$B = \frac{9}{2} \div \left(\frac{1 \times 13}{11 \times 13} + \frac{-1 \times 11}{13 \times 11} \right)$$

$$B = \frac{9}{2} \div \left(\frac{13}{143} + \frac{-11}{143} \right)$$

$$B = \frac{9}{2} \div \frac{2}{143}$$

$$B = \frac{9}{2} \times \frac{143}{2}$$

$$B =$$

$$\boxed{B = \frac{1\ 287}{4}}$$

$$C = \frac{-15}{13} - \frac{15}{104} \times \frac{-13}{9}$$

$$C = \frac{-15}{13} - \frac{5 \times 3}{-8 \times -13} \times \frac{1 \times -13}{3 \times 3}$$

$$C = \frac{-15}{13} - \frac{-5}{24}$$

$$C = \frac{-15 \times 24}{13 \times 24} - \frac{-5 \times 13}{24 \times 13}$$

$$C = \frac{-360}{312} - \frac{-65}{312}$$

$$\boxed{C = \frac{-295}{312}}$$

Corrigé de l'exercice 2

Calculer les expressions suivantes et donner le résultat sous la forme d'une fraction irréductible.

$$A = \frac{\frac{8}{5} - 1}{\frac{3}{2} - 9}$$

$$A = \frac{\frac{8}{5} - \frac{1 \times 5}{1 \times 5}}{\frac{3}{2} - \frac{9 \times 2}{1 \times 2}}$$

$$A = \frac{\frac{8}{5} - \frac{5}{5}}{\frac{3}{2} - \frac{18}{2}}$$

$$A = \frac{3}{5} \div \frac{-15}{2}$$

$$A = \frac{3}{5} \times \frac{-2}{15}$$

$$A = \frac{1 \times 3}{-5 \times -1} \times \frac{2 \times -1}{5 \times 3}$$

$$A = \boxed{\frac{-2}{25}}$$

$$B = \frac{-1}{2} \div \left(\frac{3}{11} - \frac{-9}{4} \right)$$

$$B = \frac{-1}{2} \div \left(\frac{3 \times 4}{11 \times 4} - \frac{-9 \times 11}{4 \times 11} \right)$$

$$B = \frac{-1}{2} \div \left(\frac{12}{44} - \frac{-99}{44} \right)$$

$$B = \frac{-1}{2} \div \frac{111}{44}$$

$$B = \frac{-1}{2} \times \frac{44}{111}$$

$$B = \frac{-1}{1 \times 2} \times \frac{22 \times 2}{111}$$

$$\boxed{B = \frac{-22}{111}}$$

$$C = 2 + \frac{10}{9} \div \frac{16}{9}$$

$$C = 2 + \frac{10}{9} \times \frac{9}{16}$$

$$C = 2 + \frac{5 \times 2}{1 \times 9} \times \frac{1 \times 9}{8 \times 2}$$

$$C = 2 + \frac{5}{8}$$

$$C = \frac{2 \times 8}{1 \times 8} + \frac{5}{8}$$

$$C = \frac{16}{8} + \frac{5}{8}$$

$$\boxed{C = \frac{21}{8}}$$

Corrigé de l'exercice 3

Calculer les expressions suivantes et donner le résultat sous la forme d'une fraction irréductible.

$$A = \frac{-7}{6} \times \left(\frac{-1}{2} - \frac{-13}{3} \right)$$

$$A = \frac{-7}{6} \times \left(\frac{-1 \times 3}{2 \times 3} - \frac{-13 \times 2}{3 \times 2} \right)$$

$$A = \frac{-7}{6} \times \left(\frac{-3}{6} - \frac{-26}{6} \right)$$

$$A = \frac{-7}{6} \times \frac{23}{6}$$

$$A =$$

$$\boxed{A = \frac{-161}{36}}$$

$$B = \frac{\frac{-7}{4} - 8}{\frac{-1}{2} + 2}$$

$$B = \frac{\frac{-7}{4} - \frac{8 \times 4}{1 \times 4}}{\frac{-1}{2} + \frac{2 \times 2}{1 \times 2}}$$

$$B = \frac{\frac{-7}{4} - \frac{32}{4}}{\frac{-1}{2} + \frac{4}{2}}$$

$$B = \frac{\frac{-39}{4} \div \frac{3}{2}}{\frac{-39}{4} \times \frac{2}{3}}$$

$$B = \frac{\frac{-13 \times 3}{2 \times 2} \times \frac{1 \times 2}{1 \times 3}}{\frac{-13}{2}}$$

$$\boxed{B = \frac{-13}{2}}$$

$$C = \frac{-20}{7} - \frac{16}{49} \times \frac{-21}{4}$$

$$C = \frac{-20}{7} - \frac{4 \times 4}{-7 \times 7} \times \frac{3 \times -7}{1 \times 4}$$

$$C = \frac{-20}{7} - \frac{-12}{7}$$

$$C =$$

$$C = \frac{-20}{7} - \frac{-12}{7}$$

$$\boxed{C = \frac{-8}{7}}$$

Corrigé de l'exercice 4

Calculer les expressions suivantes et donner le résultat sous la forme d'une fraction irréductible.

$$A = \frac{-26}{5} - \frac{26}{5} \div \frac{52}{25}$$

$$A = \frac{-26}{5} - \frac{26}{5} \times \frac{25}{52}$$

$$A = \frac{-26}{5} - \frac{1 \times 26}{1 \times 5} \times \frac{5 \times 5}{2 \times 26}$$

$$A = \frac{-26}{5} - \frac{5}{2}$$

$$A = \frac{-26 \times 2}{5 \times 2} - \frac{5 \times 5}{2 \times 5}$$

$$A = \frac{-52}{10} - \frac{25}{10}$$

$$\boxed{A = \frac{-77}{10}}$$

$$B = \frac{-10}{3} \div \left(\frac{-13}{10} + \frac{10}{13} \right)$$

$$B = \frac{-10}{3} \div \left(\frac{-13 \times 13}{10 \times 13} + \frac{10 \times 10}{13 \times 10} \right)$$

$$B = \frac{-10}{3} \div \left(\frac{-169}{130} + \frac{100}{130} \right)$$

$$B = \frac{-10}{3} \div \frac{-69}{130}$$

$$B = \frac{-10}{3} \times \frac{-130}{69}$$

$$B = \frac{-10}{-3 \times -1} \times \frac{130 \times -1}{69}$$

$$\boxed{B = \frac{1300}{207}}$$

$$C = \frac{\frac{-6}{5} + 6}{\frac{-7}{8} - 2}$$

$$C = \frac{\frac{-6}{5} + \frac{6 \times 5}{1 \times 5}}{\frac{-7}{8} - \frac{2 \times 8}{1 \times 8}}$$

$$C = \frac{\frac{-6}{5} + \frac{30}{16}}{\frac{-7}{8} - \frac{8}{8}}$$

$$C = \frac{\frac{5}{-7} + \frac{5}{16}}{\frac{24}{5} \div \frac{-23}{8}}$$

$$C = \frac{24}{5} \times \frac{-8}{23}$$

$$C = \frac{24}{-5 \times -1} \times \frac{8 \times -1}{23}$$

$$\boxed{C = \frac{-192}{115}}$$

Corrigé de l'exercice 5

Calculer les expressions suivantes et donner le résultat sous la forme d'une fraction irréductible.

$$A = \frac{-1}{8} \div \left(\frac{-10}{9} + \frac{7}{8} \right)$$

$$A = \frac{-1}{8} \div \left(\frac{-10 \times 8}{9 \times 8} + \frac{7 \times 9}{8 \times 9} \right)$$

$$A = \frac{-1}{8} \div \left(\frac{-80}{72} + \frac{63}{72} \right)$$

$$A = \frac{-1}{8} \div \frac{-17}{72}$$

$$A = \frac{-1}{8} \times \frac{-72}{17}$$

$$A = \frac{-1}{-1 \times 8} \times \frac{9 \times 8}{17}$$

$A = \frac{9}{17}$

$$B = \frac{-3}{8} - \frac{-3}{64} \times \frac{4}{3}$$

$$B = \frac{-3}{8} - \frac{-1 \times 3}{16 \times 4} \times \frac{1 \times 4}{1 \times 3}$$

$$B = \frac{-3}{8} - \frac{-1}{16}$$

$$B = \frac{-3 \times 2}{8 \times 2} - \frac{-1}{16}$$

$$B = \frac{-6}{16} - \frac{-1}{16}$$

$B = \frac{-5}{16}$

$$C = \frac{\frac{3}{2} + 1}{\frac{-2}{3} - 7}$$

$$C = \frac{\frac{3}{2} + \frac{1 \times 2}{1 \times 2}}{\frac{-2}{3} - \frac{7 \times 3}{1 \times 3}}$$

$$C = \frac{\frac{3}{2} + \frac{2}{2}}{\frac{-2}{3} - \frac{21}{3}}$$

$$C = \frac{5}{2} \div \frac{-23}{3}$$

$$C = \frac{5}{2} \times \frac{-3}{23}$$

$$C = \frac{5}{-2 \times -1} \times \frac{3 \times -1}{23}$$

$C = \frac{-15}{46}$

Corrigé de l'exercice 6

Calculer les expressions suivantes et donner le résultat sous la forme d'une fraction irréductible.

$$A = \frac{-1}{4} \div \left(\frac{-8}{13} + \frac{-13}{5} \right)$$

$$A = \frac{-1}{4} \div \left(\frac{-8 \times 5}{13 \times 5} + \frac{-13 \times 13}{5 \times 13} \right)$$

$$A = \frac{-1}{4} \div \left(\frac{-40}{65} + \frac{-169}{65} \right)$$

$$A = \frac{-1}{4} \div \frac{-209}{65}$$

$$A = \frac{-1}{4} \times \frac{-65}{209}$$

$$A = \frac{-1}{-4 \times -1} \times \frac{65 \times -1}{209}$$

$A = \frac{65}{836}$

$$B = \frac{\frac{7}{4} - 8}{\frac{7}{6} - 10}$$

$$B = \frac{\frac{7}{4} - \frac{8 \times 4}{1 \times 4}}{\frac{7}{6} - \frac{10 \times 6}{1 \times 6}}$$

$$B = \frac{\frac{7}{4} - \frac{32}{6}}{\frac{7}{6} - \frac{1 \times 6}{1 \times 6}}$$

$$B = \frac{\frac{4}{7} - \frac{4}{60}}{\frac{7}{6} - \frac{6}{6}}$$

$$B = \frac{\frac{-25}{4} \div \frac{-53}{6}}{\frac{-25}{4} \times \frac{-6}{53}}$$

$$B = \frac{\frac{-25}{-2 \times -2} \times \frac{3 \times -2}{53}}{\frac{-25}{53}}$$

$B = \frac{75}{106}$

$$C = \frac{90}{13} + \frac{3}{13} \times \frac{39}{50}$$

$$C = \frac{90}{13} + \frac{3}{1 \times 13} \times \frac{3 \times 13}{50}$$

$$C = \frac{90}{13} + \frac{9}{50}$$

$$C = \frac{90 \times 50}{13 \times 50} + \frac{9 \times 13}{50 \times 13}$$

$$C = \frac{4500}{650} + \frac{117}{650}$$

$C = \frac{4617}{650}$

Corrigé de l'exercice 7

Calculer les expressions suivantes et donner le résultat sous la forme d'une fraction irréductible.

$$A = \frac{-10}{7} \times \left(\frac{-6}{11} - \frac{8}{7} \right)$$

$$A = \frac{-10}{7} \times \left(\frac{-6 \times 7}{11 \times 7} - \frac{8 \times 11}{7 \times 11} \right)$$

$$A = \frac{-10}{7} \times \left(\frac{-42}{77} - \frac{88}{77} \right)$$

$$A = \frac{-10}{7} \times \frac{-130}{77}$$

$$A = \frac{-10}{-7 \times 2} \times \frac{130 \times 2}{77}$$

$$\boxed{A = \frac{1300}{539}}$$

$$B = \frac{-10}{9} + 8$$

$$B = \frac{\frac{2}{3} - 4}{\frac{3}{1}}$$

$$B = \frac{\frac{-10}{9} + \frac{8 \times 9}{1}}{\frac{2}{3} - \frac{4 \times 3}{1}}$$

$$B = \frac{\frac{-10}{9} + \frac{72}{9}}{\frac{2}{3} - \frac{12}{3}}$$

$$B = \frac{62}{9} \div \frac{-10}{3}$$

$$B = \frac{62}{9} \times \frac{-3}{10}$$

$$B = \frac{\frac{31 \times 2}{-3 \times 3}}{\frac{1 \times 3}{5 \times 2}}$$

$$\boxed{B = \frac{-31}{15}}$$

$$C = \frac{-16}{7} + \frac{-9}{28} \div \frac{-10}{21}$$

$$C = \frac{-16}{7} + \frac{-9}{28} \times \frac{-21}{10}$$

$$C = \frac{-16}{7} + \frac{-9}{-4 \times 7} \times \frac{3 \times 7}{10}$$

$$C = \frac{-16}{7} + \frac{27}{40}$$

$$C = \frac{-16 \times 40}{7 \times 40} + \frac{27 \times 7}{40 \times 7}$$

$$C = \frac{-640}{280} + \frac{189}{280}$$

$$\boxed{C = \frac{-451}{280}}$$

Corrigé de l'exercice 8

Calculer les expressions suivantes et donner le résultat sous la forme d'une fraction irréductible.

$$A = \frac{8}{3} + \frac{2}{3} \times \frac{3}{4}$$

$$A = \frac{8}{3} + \frac{1 \times 2}{1 \times 3} \times \frac{1 \times 3}{2 \times 2}$$

$$A = \frac{8}{3} + \frac{1}{2}$$

$$A = \frac{8 \times 2}{3 \times 2} + \frac{1 \times 3}{2 \times 3}$$

$$A = \frac{16}{6} + \frac{3}{6}$$

$$\boxed{A = \frac{19}{6}}$$

$$B = \frac{\frac{-2}{5} - 10}{\frac{-7}{9}}$$

$$B = \frac{\frac{-2}{5} - \frac{10 \times 5}{1}}{\frac{-7}{9} + \frac{5 \times 9}{1}}$$

$$B = \frac{\frac{-2}{5} - \frac{50}{1}}{\frac{-7}{9} + \frac{45}{9}}$$

$$B = \frac{\frac{-52}{5} \div \frac{38}{9}}{\frac{-52}{5} \times \frac{9}{38}}$$

$$B = \frac{\frac{-26 \times 2}{5} \times \frac{9}{19 \times 2}}{\frac{-234}{95}}$$

$$C = \frac{-7}{6} \div \left(\frac{5}{13} + \frac{13}{4} \right)$$

$$C = \frac{-7}{6} \div \left(\frac{5 \times 4}{13 \times 4} + \frac{13 \times 13}{4 \times 13} \right)$$

$$C = \frac{-7}{6} \div \left(\frac{20}{52} + \frac{169}{52} \right)$$

$$C = \frac{-7}{6} \div \frac{189}{52}$$

$$C = \frac{-7}{6} \times \frac{52}{189}$$

$$C = \frac{-1 \times 7}{3 \times 2} \times \frac{26 \times 2}{27 \times 7}$$

$$\boxed{C = \frac{-26}{81}}$$

Corrigé de l'exercice 9

Calculer les expressions suivantes et donner le résultat sous la forme d'une fraction irréductible.

$$A = \frac{25}{3} + \frac{20}{9} \div \frac{-5}{6}$$

$$A = \frac{25}{3} + \frac{20}{9} \times \frac{-6}{5}$$

$$A = \frac{25}{3} + \frac{4 \times 5}{-3 \times -3} \times \frac{2 \times -3}{1 \times 5}$$

$$A = \frac{25}{3} + \frac{-8}{3}$$

$$A =$$

$$A = \frac{25}{3} + \frac{-8}{3}$$

$$\boxed{A = \frac{17}{3}}$$

$$B = \frac{-1}{2} \times \left(\frac{1}{9} + \frac{-1}{11} \right)$$

$$B = \frac{-1}{2} \times \left(\frac{1 \times 11}{9 \times 11} + \frac{-1 \times 9}{11 \times 9} \right)$$

$$B = \frac{-1}{2} \times \left(\frac{11}{99} + \frac{-9}{99} \right)$$

$$B = \frac{-1}{2} \times \frac{2}{99}$$

$$B = \frac{-1}{1 \times 2} \times \frac{1 \times 2}{99}$$

$$\boxed{B = \frac{-1}{99}}$$

$$C = \frac{\frac{5}{2} - 9}{\frac{-7}{3} + 5}$$

$$C = \frac{\frac{5}{2} - \frac{9 \times 2}{1 \times 2}}{\frac{-7}{3} + \frac{5 \times 3}{1 \times 3}}$$

$$C = \frac{\frac{5}{2} - \frac{18}{2}}{\frac{-7}{3} + \frac{15}{3}}$$

$$C = \frac{\frac{-13}{2} \div \frac{8}{3}}{\frac{-13}{2} \times \frac{3}{8}}$$

$$C =$$

$$\boxed{C = \frac{-39}{16}}$$

Corrigé de l'exercice 10

Calculer les expressions suivantes et donner le résultat sous la forme d'une fraction irréductible.

$$A = \frac{5}{2} + \frac{-25}{8} \times \frac{24}{5}$$

$$A = \frac{5}{2} + \frac{-5 \times 5}{1 \times 8} \times \frac{3 \times 8}{1 \times 5}$$

$$A = \frac{5}{2} + -15$$

$$A = \frac{5}{2} + \frac{-15 \times 2}{1 \times 2}$$

$$A = \frac{5}{2} + \frac{-30}{2}$$

$$\boxed{A = \frac{-25}{2}}$$

$$B = \frac{\frac{5}{7} - 1}{\frac{3}{4} - 9}$$

$$B = \frac{\frac{5}{7} - \frac{1 \times 7}{1 \times 7}}{\frac{3}{4} - \frac{9 \times 4}{1 \times 4}}$$

$$B = \frac{\frac{5}{7} - \frac{7}{7}}{\frac{3}{4} - \frac{36}{4}}$$

$$B = \frac{-2}{7} \div \frac{-33}{4}$$

$$B = \frac{-2}{7} \times \frac{-4}{33}$$

$$B = \frac{-2}{-7 \times -1} \times \frac{4 \times -1}{33}$$

$$\boxed{B = \frac{8}{231}}$$

$$C = \frac{-1}{5} \div \left(\frac{-7}{12} + \frac{9}{5} \right)$$

$$C = \frac{-1}{5} \div \left(\frac{-7 \times 5}{12 \times 5} + \frac{9 \times 12}{5 \times 12} \right)$$

$$C = \frac{-1}{5} \div \left(\frac{-35}{60} + \frac{108}{60} \right)$$

$$C = \frac{-1}{5} \div \frac{73}{60}$$

$$C = \frac{-1}{5} \times \frac{60}{73}$$

$$C = \frac{-1}{1 \times 5} \times \frac{12 \times 5}{73}$$

$$\boxed{C = \frac{-12}{73}}$$

Corrigé de l'exercice 11

Calculer les expressions suivantes et donner le résultat sous la forme d'une fraction irréductible.

$$A = \frac{3}{10} \times \left(\frac{-11}{6} + \frac{-4}{5} \right)$$

$$A = \frac{3}{10} \times \left(\frac{-11 \times 5}{6 \times 5} + \frac{-4 \times 6}{5 \times 6} \right)$$

$$A = \frac{3}{10} \times \left(\frac{-55}{30} + \frac{-24}{30} \right)$$

$$A = \frac{3}{10} \times \frac{-79}{30}$$

$$A = \frac{1 \times 3}{-10 \times 1} \times \frac{79 \times 1}{10 \times 3}$$

$$\boxed{A = \frac{-79}{100}}$$

$$B = \frac{\frac{9}{2} + 1}{\frac{-9}{4} + 7}$$

$$B = \frac{\frac{9}{2} + \frac{1 \times 2}{1 \times 2}}{\frac{-9}{4} + \frac{7 \times 4}{1 \times 4}}$$

$$B = \frac{\frac{9}{2} + \frac{2}{2}}{\frac{-9}{4} + \frac{28}{4}}$$

$$B = \frac{11}{2} \div \frac{19}{4}$$

$$B = \frac{11}{2} \times \frac{4}{19}$$

$$B = \frac{11}{1 \times 2} \times \frac{2 \times 2}{19}$$

$$\boxed{B = \frac{22}{19}}$$

$$C = \frac{12}{7} - \frac{-5}{7} \times \frac{7}{2}$$

$$C = \frac{12}{7} - \frac{-5}{1 \times 2} \times \frac{1 \times 7}{2}$$

$$C = \frac{12}{7} - \frac{-5}{2}$$

$$C = \frac{12 \times 2}{7 \times 2} - \frac{-5 \times 7}{2 \times 7}$$

$$C = \frac{24}{14} - \frac{-35}{14}$$

$$\boxed{C = \frac{59}{14}}$$

Corrigé de l'exercice 12

Calculer les expressions suivantes et donner le résultat sous la forme d'une fraction irréductible.

$$A = \frac{\frac{-1}{8} - 9}{\frac{4}{5} + 2}$$

$$A = \frac{\frac{-1}{8} - \frac{9 \times 8}{1 \times 8}}{\frac{4}{5} + \frac{2 \times 5}{1 \times 5}}$$

$$A = \frac{\frac{-1}{8} - \frac{72}{8}}{\frac{4}{5} + \frac{10}{5}}$$

$$A = \frac{\frac{-73}{8} \div \frac{14}{5}}{\frac{4}{5} + \frac{10}{5}}$$

$$A = \frac{\frac{-73}{8} \times \frac{5}{14}}{\frac{4}{5} + \frac{10}{5}}$$

$$A =$$

$$\boxed{A = \frac{-365}{112}}$$

$$B = \frac{3}{4} \times \left(\frac{7}{11} + \frac{-9}{8} \right)$$

$$B = \frac{3}{4} \times \left(\frac{7 \times 8}{11 \times 8} + \frac{-9 \times 11}{8 \times 11} \right)$$

$$B = \frac{3}{4} \times \left(\frac{56}{88} + \frac{-99}{88} \right)$$

$$B = \frac{3}{4} \times \frac{-43}{88}$$

$$B = \frac{3}{-4 \times 21} \times \frac{43 \times 1}{88}$$

$$\boxed{B = \frac{-129}{352}}$$

$$C = \frac{48}{7} + \frac{-24}{7} \div \frac{-72}{7}$$

$$C = \frac{48}{7} + \frac{-24}{7} \times \frac{-7}{72}$$

$$C = \frac{48}{7} + \frac{-1 \times 24}{-1 \times 7} \times \frac{1 \times 7}{3 \times 24}$$

$$C = \frac{48}{7} + \frac{1}{3}$$

$$C = \frac{48 \times 3}{7 \times 3} + \frac{1 \times 7}{3 \times 7}$$

$$C = \frac{144}{21} + \frac{7}{21}$$

$$\boxed{C = \frac{151}{21}}$$